

SCALING AND MODELLING LAWS IN TWO-PHASE FLOW AND BOILING HEAT TRANSFER

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ABSTRACT. In two-phase flow scaling is much more limited to very narrowly defined physical phenomena than in single phase fluids. For complex and combined phenomena it can be achieved not by using dimensionless numbers alone but in addition a detailed mathematical description of the physical problem - usually in the form of a computer program - must be available. An important role plays the scaling of the thermodynamic data of the modelling fluid. From a literature survey and from own scaling experiments the conclusion can be drawn that Freon is a quite suitable modelling fluid for scaling steam - water mixtures. However, without a theoretical description of the phenomena nondimensional numbers for scaling two-phase flow must be handled very carefully.

1. INTRODUCTION

The transfer of experimental results obtained under scaled conditions to the reality in an industrial plant is an old problem of engineering. There must be a sufficient similarity of the main parameters influencing the precedents in the test equipment and in the original set-up. This similarity can be of geometrical, mechanical, static, dynamic, thermal, thermodynamic, electrical and mechanical nature.

In single phase hydrodynamics and heat transfer we are accustomed to use scaling and modelling laws since many years. The occurrences are analogous in a diabatic flow if

- the velocity field,
- the temperature field and
- the pressure field (supersonic flow)

are similar. Only regarding subsonic flow the velocity and temperature fields are described by the well-known constitution laws for mass, energy and momentum. From these laws dimensionless numbers like

$$\frac{x}{l}, \frac{y}{l}, \frac{z}{l}$$

$$Re = \frac{w \cdot l}{\nu}, \quad Fr = \frac{w^2}{g l}, \quad Eu = \frac{\Delta p}{\rho w^2}$$

$$Nu = \frac{\alpha \cdot l}{\lambda}, \quad Gr = \frac{l^3 g \beta \Delta T}{\nu^2}, \quad Pr = \frac{\eta \cdot c}{\lambda}$$

are derived and similarity is assumed, if these dimensionless numbers are identical in the test and in the original conditions. Usually it is easy to guarantee the geometrical similarity by choosing the same ratios of length x/l , y/l , z/l , i.e. to make all dimensions of the test object proportional to a characteristic length l of the original set-up. The other dimensionless numbers represent ratios of forces or of energies (e.g. the Nusselt-number) which cannot be made identical in the model and in the original as it can easily be seen from the different exponents of the parameters. The velocity is in the Reynolds-number of the first power and in the Froude-number of the second one. The Reynolds-number is the ratio of inertia and viscous forces and the Froude-number contains the buoyancy force. This means, that in mixed convection either the forced flow or the buoyant induced one can be scaled only. In addition the velocity and the temperature field is influenced by the thermodynamic properties - in single phase flow mainly the viscosity, density, specific heat and thermal conductivity. By comparing the behaviour of different fluids not all these properties can be exactly scaled in general.

The velocity and the temperature field can be described by functions of the form

$$\frac{w}{w_0} = f_w \left(\frac{x}{l}, \frac{y}{l}, \frac{z}{l}, Re, Pr, Gr \right) \quad (1)$$

$$\frac{T}{T_0} = f_T \left(\frac{x}{l}, \frac{y}{l}, \frac{z}{l}, Re, Pr, Gr \right) \quad (2)$$

$$Nu = f_\alpha (Re, Pr, Gr) \quad (3)$$

and in practice we rule out one of the dimensionless numbers, i.e. the Reynolds-number or the Grashof-number depending whether forced or free convection prevails. Therefore already in single phase flow scaling or similarity laws have a restricted and only approximate validity. This we have to keep in mind when we now discuss similarity in two-phase flow and in boiling heat transfer.

2. DIMENSIONLESS NUMBERS FOR TWO-PHASE FLOW AND BOILING HEAT TRANSFER

From a theoretical point of view it is the best and most exact procedure to derive the dimensionless numbers from differential equations completely describing the interesting physical phenomenon by arranging the terms in a certain way. Another systematic procedure is to form a matrix from the exponents of the influencing parameters and their dimensions as indicated in fig. 1. The number of the influencing parameters minus the rank of the matrix gives the number of the dimensionless groups and these again can be elaborated by evaluating the matrix. Finally a third possibility to obtain dimensionless numbers is the method of trial and error by multiplying and dividing selected parameters.

By these methods or sometimes just by intuitive experience several dimensionless numbers were found for two-phase flow and for thermohydraulic processes with phase change already several years ago. Fig. 2 gives some examples of them. They are usually restricted to a single phenomenon for example the Weber-number to droplet formation or the Jakob-number to the heat flux ratio in the

$$F = w^a ; \Delta p^b ; l^c ; \rho^d ; \eta^e$$

$$\left(\frac{m}{s}\right)^a ; \left(\frac{kg}{ms^2}\right)^b ; (m)^c ; \left(\frac{kg}{m^3}\right)^d ; \left(\frac{kg}{ms}\right)^e$$

mass (kg)	0	b	0	d	e	...
length (m)	a	-b	c	-3d	-e	...
time (s)	-a	-2b	0	0	-e	...
⋮	⋮	⋮	⋮	⋮	⋮	⋮

or

	a	b	c	d	e	...
kg	0	1	0	1	1	...
m	1	-1	1	-3	-1	...
s	-1	-2	0	0	-1	...
⋮	⋮	⋮	⋮	⋮	⋮	⋮

Fig. 1. Matrix for forming dimensionless groups.

Weber number:

$$We = \frac{\rho \cdot d_d \cdot w^2}{\sigma}$$

Laplace constant:

$$La = \frac{\sigma}{g(\rho_l - \rho_g)} \quad [m^2]$$

Jakob number:

$$Ja = \frac{c \cdot \rho_l (\vartheta_w - \vartheta_{bulk})}{h_{lg} \cdot \rho_g}$$

Bubble Reynolds number:

$$Re_b = \frac{\rho_g \cdot w_b \cdot d_b}{\eta_g}$$

Boiling number:

$$N_{Bo} = \frac{q}{h_{lg} \cdot \rho_g \cdot w_g}$$

Buoyancy number:

$$N_{Bu} = \frac{\rho_l - \rho_g}{\rho_l}$$

Subcooling number:

$$N_{sub} = \frac{\Delta h_{sub} \cdot (\rho_l - \rho_g)}{h_{lg} \cdot \rho_g}$$

Phase change number:

$$N_{ph} = \frac{\dot{m}_g \cdot (\rho_l - \rho_g) \cdot l}{\rho_g \cdot \rho_l \cdot w_l}$$

Slip ratio

$$s = \frac{w_g}{w_l}$$

Drift number

$$N_D = \frac{w_{g, surface}}{w_{l, surface}}$$

Martinelli parameter:

$$X = \left(\frac{\rho_g}{\rho_l} \right)^{0.5} \cdot \left(\frac{\eta_l}{\eta_g} \right)^{0.1} \cdot \left(\frac{1-x}{x} \right)^{0.9}$$

Fig. 2. Examples for dimensionless numbers in two-phase systems.

liquid and in the vapour from the wall. A special role plays the Martinelli parameter X which was found by Martinelli studying two-phase pressure drop but which seems to have a much more general validity.

In single phase, single component systems only the velocity and the temperature field have to be regarded but in two-phase flow in addition we have to take into account the density distribution - i.e. the void fraction or the quality - in the system. Finally in a multi-component system the concentration field would have to be added. This influence we do not want to follow up in our discussion. So in two-phase flow with and without boiling we must have information on

the velocity field,
the phase distribution field and
the temperature field.

The last one usually can be neglected if we have a one component two-phase system in thermodynamic equilibrium.

The second phase brings with it a lot of complications in our similarity or scaling deliberations. The hydrodynamic and thermodynamic properties in both phases have to be similar and also the phase change behaviour must be comparable. Before dis-

cussing, whether these conditions are compatible we have briefly to think about, why and what do we want to scale in two-phase flow:

in single phase flow usually we have the problem of scaling the size of an apparatus or of a plant, that is we do the experiments with small, scaled down objects. In two-phase flow there is the question of the proportion too, but a much more severe problem rises from the very large heat input, which is needed to do two-phase and boiling experiments. One would need for example several MW to make heat transfer experiments with a representative section of a nuclear reactor fuel element. A geometrically scaling down of the fuel rod array is almost not possible because the bubbles keep their size and the ratio between bubble diameter and rod space would change and so seriously influence the boiling phenomena. There is another possibility to reduce the power input by using instead of water a modelling liquid with low latent heat of evaporation. And so in two-phase flow not so much a scaling of the geometry but a scaling of the fluid is of interest and importance.

Due to the fact that thermodynamic properties of the gases and the liquid phase of the modelling fluid play an important role, it is essential that

1. these properties are well known and
2. that they show a similar behaviour as the original fluid.

Besides water the refrigerants (Freon R11, R12, R113) are pretty well researched and have well known thermodynamic properties. In addition they offer convenient experimental conditions with respect to pressure and temperature.

3. THERMODYNAMIC SCALING OF THE FLUIDS

From a very first point of view the claim to the similarity of the thermodynamic conditions seems simply to be solved by selecting the thermodynamic state of the modelling fluid, in such a way that the important influencing properties are comparable. This can completely be done for one property, but for the others only approximatively. So we find very often in the literature that in the scaling tests the thermodynamic state of the modelling fluid is so selected that the density ratio ρ_f/ρ_g between liquid and vapour is the same in the model and in the original. This may be a very serious restriction because there can be other properties as important as the density.

If there would be a common equation of state for both liquids which we could write in a dimensionless reduced form

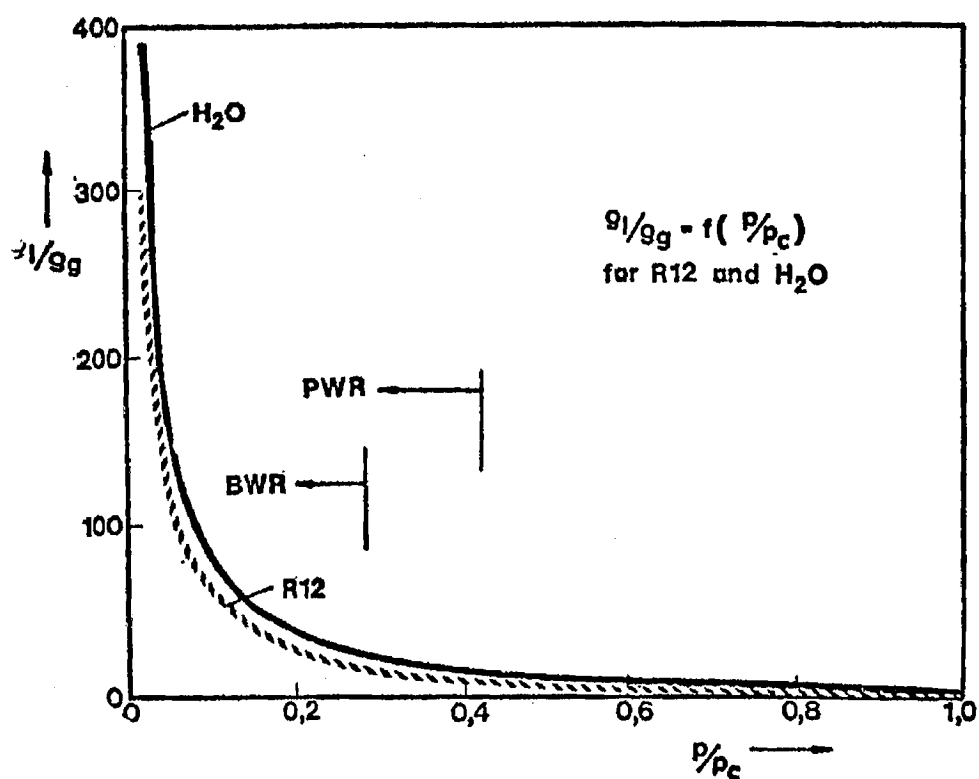


Fig. 3. Density ratio ρ_l/ρ_g of water and Freon 12 as function of reduced pressure.

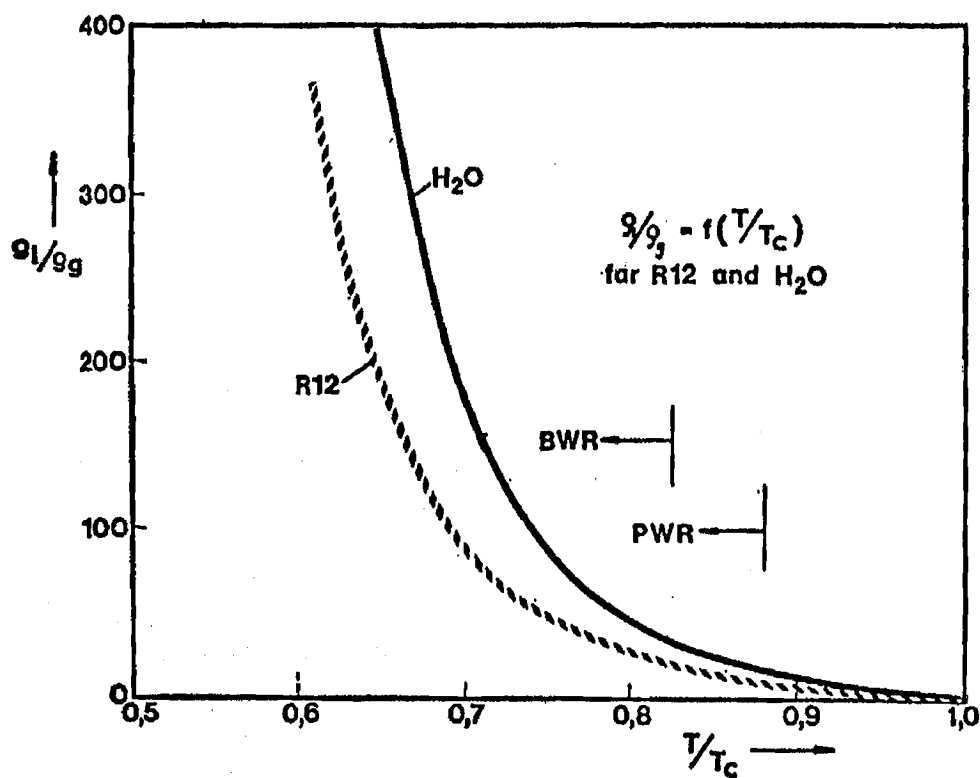


Fig. 4. Density ratio ρ_l/ρ_g of water and Freon 12 as function reduced temperature.

with the help of the thermodynamic consistency we could make use of the thermodynamic theorem of corresponding states. One of the simplest equations of state is certainly the Van der Waals-equation, which we can write as follows:

$$\left(\frac{p}{p_c} + \frac{3}{v_{v_c}}\right) \left(3 \frac{v}{v_c} - 1\right) = 8 \frac{T}{T_c} \quad (4)$$

In this form - which is reduced with the critical data - the Van der Waals-equation contains only universal constants not restricted to a certain liquid. Certainly the Van der Waals-equation allows only a very rough and unprecise prediction of the thermodynamic properties of Freon. But it gives the hint that the critical data p_c , T_c and v_c may be useful to get a corresponding state for comparable thermal, caloric and even transport properties, since, as Grigull [1] showed there is according to the thermodynamic consistency a strong familiarity between transport data and certain caloric properties.

In a single component system the two phases can only exist along the saturation line which means that one thermodynamic property fixes the whole state. So using the critical properties we can either scale with the critical pressure ratio

$$\left(\frac{p}{p_c}\right)_{\text{Original}} = \left(\frac{p}{p_c}\right)_{\text{Modell}} \quad (5)$$

or with any other critical ratio like

$$\left(\frac{T}{T_c}\right)_0 = \left(\frac{T}{T_c}\right)_M, \left(\frac{p}{p_c}\right)_0 = \left(\frac{p}{p_c}\right)_M, \left(\frac{\eta}{\eta_c}\right)_0 = \left(\frac{\eta}{\eta_c}\right)_M \quad (6)$$

Comparisons have proved that the pressure ratio is the most useful parameter for many applications especially for scaling between water and Freon. As shown in fig. 3 there is only a deviation of a few percent in the density ratio ρ_l/ρ_g of liquid and vapour for water and Freon if we scale it with the critical pressure ratio. This again means scaling with p/p_c and with ρ_l/ρ_g give almost the same results. This is not the case if we use instead of the pressure ratio the critical temperature ratio as it can be seen from fig. 4.

In many hydrodynamic and heat transfer problems the density ratio may play the important role but there are other problems like bubble formation, flashing, entrainment and so on, where other properties as surface tension, viscosity, thermal conductivity are governing the phenomenon. A comparison of some properties scaled with the critical pressure ratio is given in fig. 5, where data for viscosity, thermal conductivity, surface tension, Prandtl-number and latent heat of evaporation are

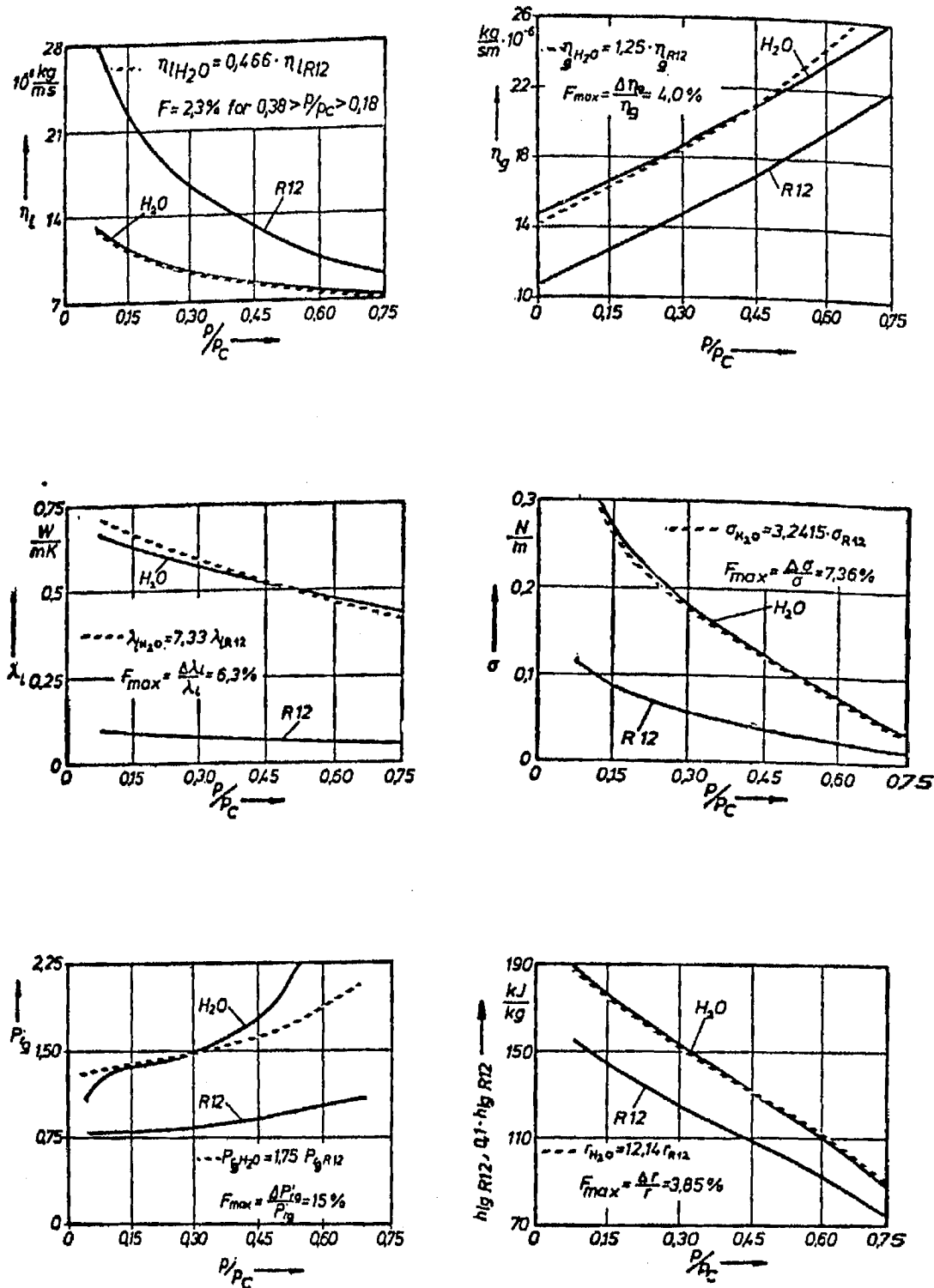


Fig. 5. Comparison of thermodynamic and transport properties of water and Freon 12.

plotted. We see that the absolute values of these data for water and for Freon differ considerably. But we can transduce the Freon data to the water data by simply multiplying with an individual factor as demonstrated with the dotted lines in fig. 5. This factor then has to be taken in account also in the fluiddynamic scaling. If we deduce the mass flow rate for the

modelling conditions with the help of the Reynolds-number for example we get the condition

$$Re = \frac{\dot{m}d}{\eta} ; Re_0 = Re_M ; \dot{m}_M = \dot{m}_0 \frac{\eta_M}{\eta_0} = k \cdot \dot{m}_0 \cdot \eta_M \quad (7)$$

where the factor k according to fig. 5 would be $k_1 = 2,15$ and $k_g = 0,8$. In two-phase flow, even for this simple problem, we therefore have two correction factors one for the liquid and an other one for the gaseous phase. One therefore has to decide which phase is the more important one for the special fluid dynamic process we are interested in. For scaling mass flow rate in two-phase flow we can primarily only use the viscosity either of the liquid or of the gas. For the ratio of liquid and vapour mass flow rate an additional condition exists namely the quality x for the void fraction ϵ . That means we have to neglect the influence of the viscosity of one of the phases. Already from this simple example we see that for two-phase scaling we have to subdivide in primary and secondary parameters to a much greater extend than we are used to do in single phase flow.

In transient conditions, for example with flashing in a sea-water desalination plant or during a loss of coolant accident in a water-cooled nuclear reactor, we need the first derivatives with respect to pressure of some thermodynamic properties in addition. As shown in fig. 6 also these derivatives can be made coincident by a simple multiplying factor.

A similar comparison of thermodynamic properties as discussed here but restricted to the surface tension and the viscosity can be found in a paper by Baker [2] who introduced

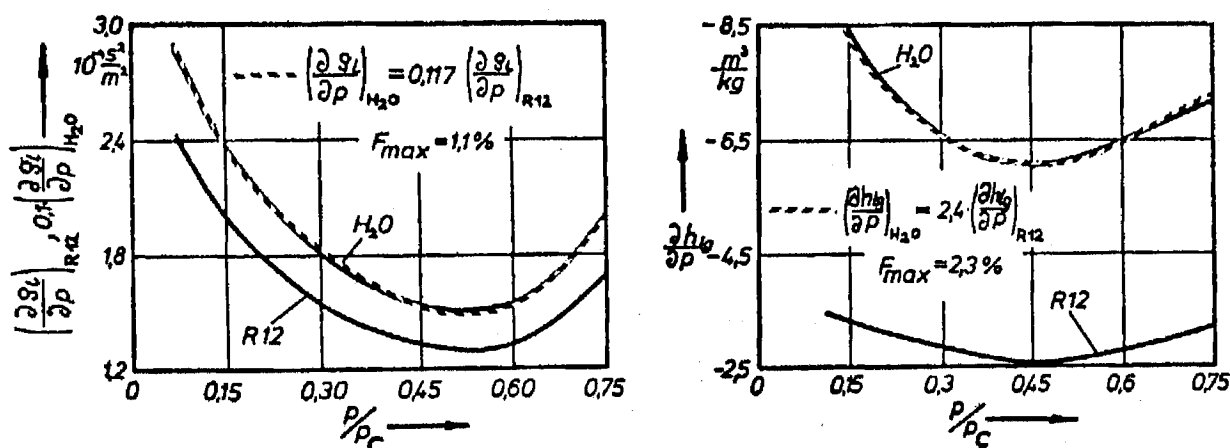


Fig. 6. Comparison of derived thermodynamic properties (water and Freon 12).

empirical reference values for surface tension and viscosity. A more detailed comparison is given in Belda's thesis [3].

4. SCALING OF SIMPLE FLUID DYNAMIC OCCURANCES

In scaling we have to distinct two steps, namely

1. to select the conditions in the mould and
2. to transfer the results obtained in the test model to original conditions.

Under simple circumstances both steps can be made with the help of dimensionless numbers as well known for pressure drop and heat transfer problems in single phase flow. For more complicated cases the dimensionless numbers give us the approximate hydrodynamic and thermodynamic conditions for running the tests and the transfer has to be made by the help of a detailed mathematical description of the physical phenomena for example in the form of differential equations integrated in a numerical way. Let us first discuss examples of more simple fluid dynamic occurances.

A first step in studying two-phase flow is the investigation of the flow pattern, i.e. the distribution of the two phases in any cross sections of the channel. Quandt [4] deduced predictions for flow pattern from the deliberation, that the forces acting in the flow must be responsible for the phase distribution. If the forces induced by the pressure drop prevail, annular flow should be present and if the surface tension becomes greater than the forces resulting from the pressure drop and from the buoyancy there should be bubble flow. From these simple ratios of the forces we can derive dimensionless numbers as for example

$$N_{\text{anular flow}} = \frac{\rho w^2 d}{\sigma} \quad (8a)$$

$$N_{\text{bubble flow}} = \frac{\sigma}{\rho g d^2} \quad (8b)$$

where equation 8a is the ratio of the inertia and surface tension forces and equation 8b is the ratio of the surface tension and the buoyancy forces. Equation 8a is nothing else than the well-known Weber-number and equation 8b represents the product of the Laplace-constant and a characteristic length for example the bubble diameter. Unfortunately the method of Quandt was not very successful in predicting the regimes of the different flow pattern. For horizontal flow another procedure for the prediction

of flow pattern was proposed by Baker. He defined the two property parameters

$$\psi = \left(\frac{\sigma_{H_2O}}{\sigma} \right) \left[\frac{\eta_L}{\eta_{H_2O}} \left(\frac{\rho_{H_2O}}{\rho_l} \right)^2 \right] \quad (9a)$$

$$\lambda = \left[\left(\frac{\rho_g}{\rho_{air}} \right) \left(\frac{\rho_l}{\rho_{H_2O}} \right) \right]^{0.5} \quad (9b)$$

and plotted a flow regime map with $1/x = \dot{M}_l/\dot{M}_g$ and the mass flow rate of the gas as additional parameters as shown in fig. 7. The terms in equation 9a und 9b are not dimensionless but we can regard them as a scaling help. For vertical flow often the flow regime map by Bennett [5] is used. Zetzmann [6] demonstrated that simply by modifying the abscissa of this diagram with the critical pressure ratio the flow regime map can be generalized for different fluids and pressures as shown in fig. 8.

A little more difficult to survey is the picture in the case of the void fraction ϵ and the slip ratio s which are closely connected if the quality x is given.

$$s = \frac{1-\epsilon}{\epsilon} \frac{\dot{x}}{1-\dot{x}} \frac{\rho_l}{\rho_g} \quad (10)$$

The slip ratio and through it the void fraction are influenced by the buoyancy forces and by the pressure drop in the channel. So empirical correlations for predicting void fraction, e.g. given by Kowalczewski [7] or by Kütükcüoğlu [8] contain

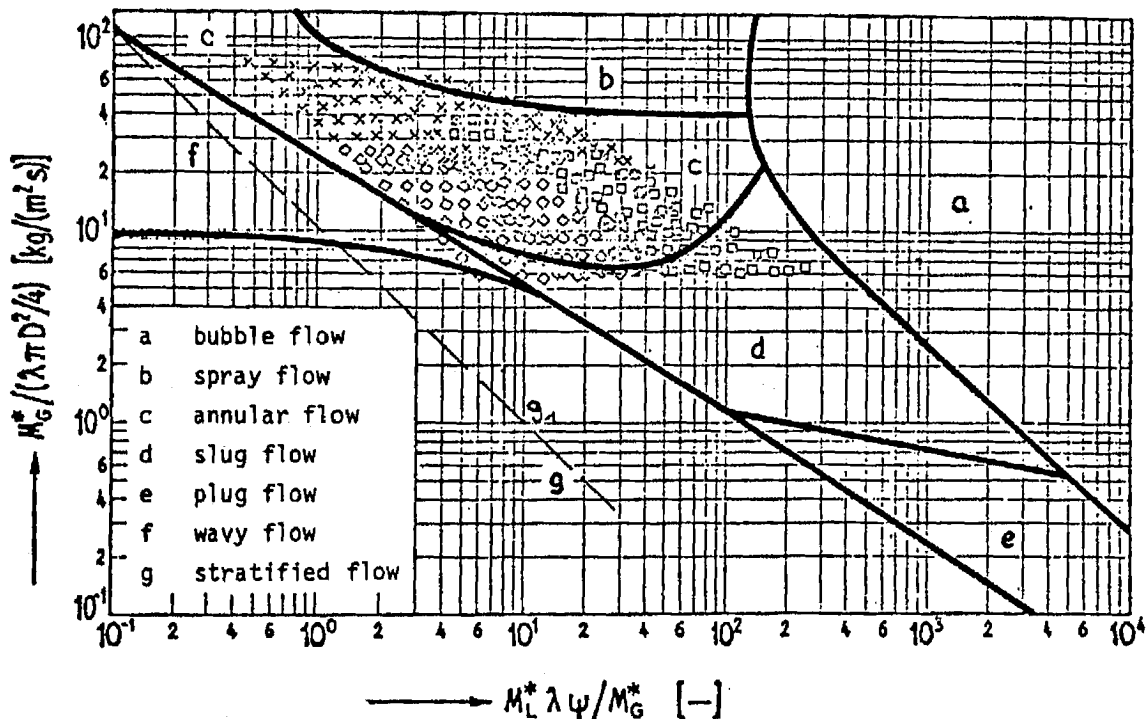


Fig. 7. Flow pattern map according to Baker [2].

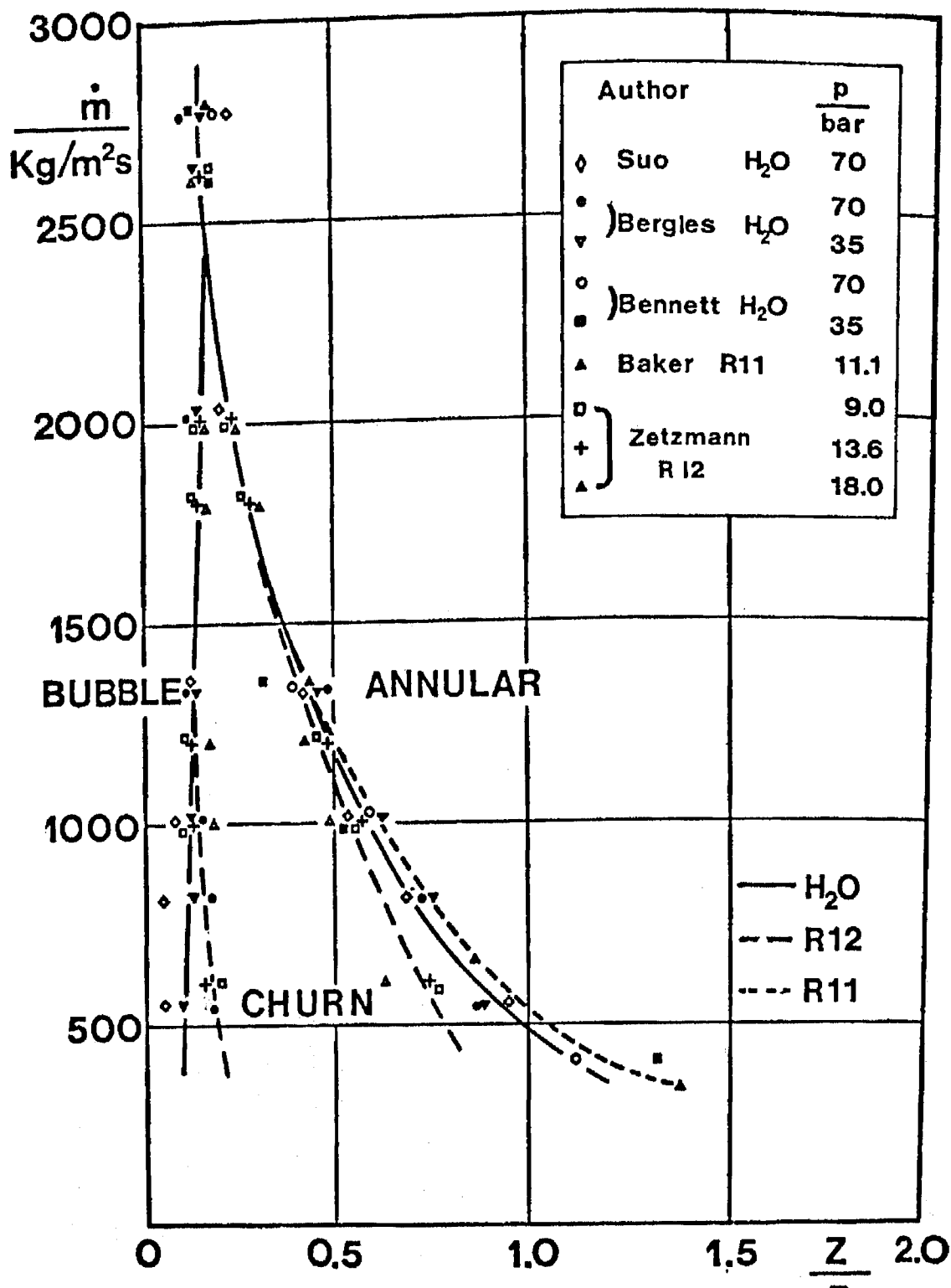


Fig. 8. Bennett's flow pattern map, modified according to Zetzmann [6].

the Froude-number

$$Fr = \frac{\dot{m}^2}{g \cdot d_h \cdot \rho_l^2} \quad (11)$$

as scaling parameter. Hewitt used the Martinelli-parameter

$$X = \sqrt{\frac{(\Delta P / \Delta l)_l}{(\Delta P / \Delta l)_g}} = \left(\frac{\rho_g}{\rho_l}\right)^{0.5} \cdot \left(\frac{\eta_l}{\eta_g}\right)^{0.1} \cdot \left(\frac{1-\dot{x}}{\dot{x}}\right)^{0.9} \quad (12)$$

for his void correlation. That means for doing modelling tests we would have to adapt either the Froude-number or the Martinelli-parameter. But both correlations do not claim general validity for a variety of fluids.

A first but very promising step for generalizing the prediction of void fraction was done by Nabizadeh [9]. Starting from the equation of Zuber and Findlay [10]

$$\epsilon = \frac{\dot{x}}{\rho_g} \left[C_0 \left(\frac{\dot{x}}{\rho_g} + \frac{1-\dot{x}}{\rho_l} \right) + \frac{1.18}{\dot{m}} \left(\frac{\sigma \cdot g (\rho_l - \rho_g)}{\rho_l^2} \right)^{0.25} \right]^{-1} \quad (13)$$

and supported by a large number of reliable own measurements he developed an empirical correlation for the C_0 -factor in Zuber-Findlay's equation of the form

$$C_0 = \left(1 + \frac{1-\dot{x}}{\dot{x}} \cdot \frac{\rho_g}{\rho_l} \right)^{-1} \left[1 + \frac{1}{n} Fr^{-0.1} \cdot \left(\frac{\rho_g}{\rho_l} \right)^n \cdot \left(\frac{1-\dot{x}}{\dot{x}} \right)^{\frac{11n}{9}} \right] \quad (14)$$

$$n = \sqrt{0.6 \frac{\rho_l - \rho_g}{\rho_l}} \quad (15)$$

Applying this extended and improved Zuber's-Findlay equation he gets quite good agreement between correlated and measured data for water, Freon 12 and Freon 113 as it can be seen from fig. 9. However, we cannot immediately deduce the parameters of a model test for given conditions of an original from equation 13 und 14 before looking to the magnitude of influence of the different terms. Nabizadeh points out that it is sufficient to adjust the same values of the density ratio of the quality and of the total mass flow density $\dot{m}$ in the model and in the original plant.

For pressure drop scaling very early a first step was done by Martinelli [11]. He gave a simple correlation between the two-phase multiplier Φ^2

$$\left(\frac{\Delta p}{\Delta l} \right)_{2ph} = \Phi_l^2 \left(\frac{\Delta p}{\Delta l} \right)_{l \text{ only}} \quad (16)$$

$$\left(\frac{\Delta p}{\Delta l} \right)_{2ph} = \Phi_g^2 \left(\frac{\Delta p}{\Delta l} \right)_{g \text{ only}}$$

and the parameter X defined by himself and already mentioned in equation 12.

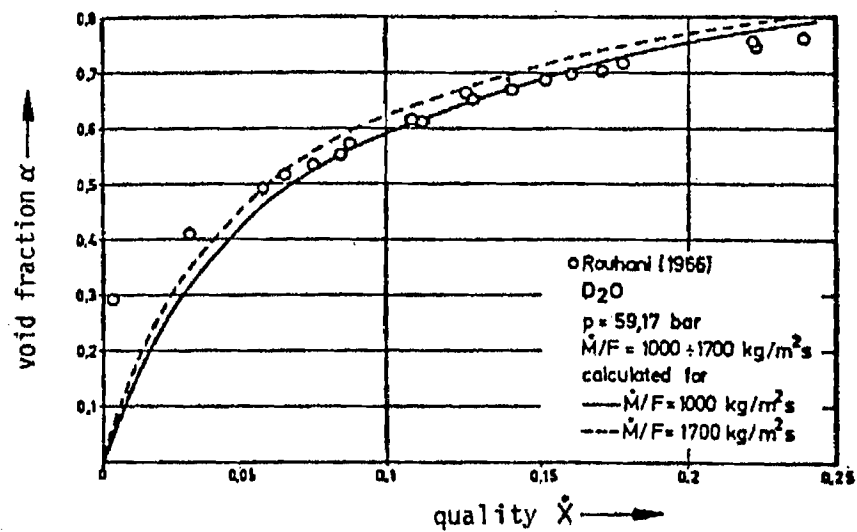
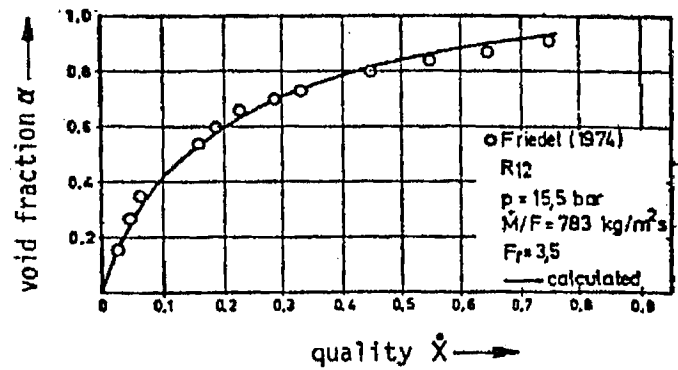
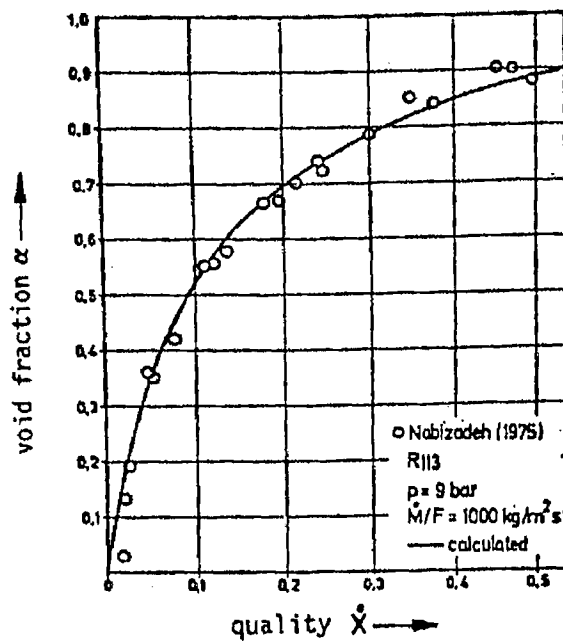


Fig. 9. Void fraction, comparison of water and Freon data, scaled with Zuber-Findlay's equation [10] modified by Nabizadeh [9].

In a detailed experimental and theoretical analysis Friedel [12] elaborated scaling rules and dimensionless numbers for two-phase pressure drop. His measurements prove that the two-phase multiplier (equation 16) is the same in water and in Freon if the following dimensionless groups are equal under test and under layout conditions.

$$\left. \frac{(\eta_l/\eta_g)^{0.2}}{(\rho_l/\rho_g)^{0.9}} \right|_O = \left. \frac{(\eta_l/\eta_g)^{0.2}}{(\rho_l/\rho_g)^{0.9}} \right|_M \quad (17)$$

$$\left. \frac{Fr_l}{Re_l^{0.25}} \right|_O = k \left. \frac{Fr_l}{Re_l^{0.25}} \right|_M \quad (18) \quad \dot{x}|_O = \dot{x}|_M$$

The second group with the Froude- and the Reynold-number contains a scaling factor k which is a slight function of the pressure and varies between 1.68 and 1.75. With good approximation for k the value 1.7 can be taken. Friedel adapts the thermodynamic state by choosing the same viscosity/density-ratio in the model and in the original. Then the mass flow rate in the test is fixed by the scaling factor k via the Reynold-number of the liquid. Proceeding so measured data in water and in Freon fall along the same line as demonstrated in fig. 10, where the two-phase multiplier is plotted versus the quality x .

Regarding heat transfer in two-phase flow we have to distinct several regions

- a first one, in which bubbles are formed at the heated wall with low quality in the fluid,
- a second one with a thin liquid film at the wall and evaporation at the phase boundary between the liquid film and the gaseous bulk flow,
- a third one with a vapour film at the wall, which the liquid cannot wet and low quality in the fluid and
- a fourth one, where the liquid cannot wet the wall too, but where the fluid is mainly vapour containing a minor quantity of liquid in form of droplets.

Heat transfer with bubble formation at the wall is a function of the heat flux density and as a generalizing parameter sometimes the Laplace-constant (see fig. 2) is used. The whole bubble boiling process is up to now not well enough understood to derive reliable scaling laws. In the high quality region the

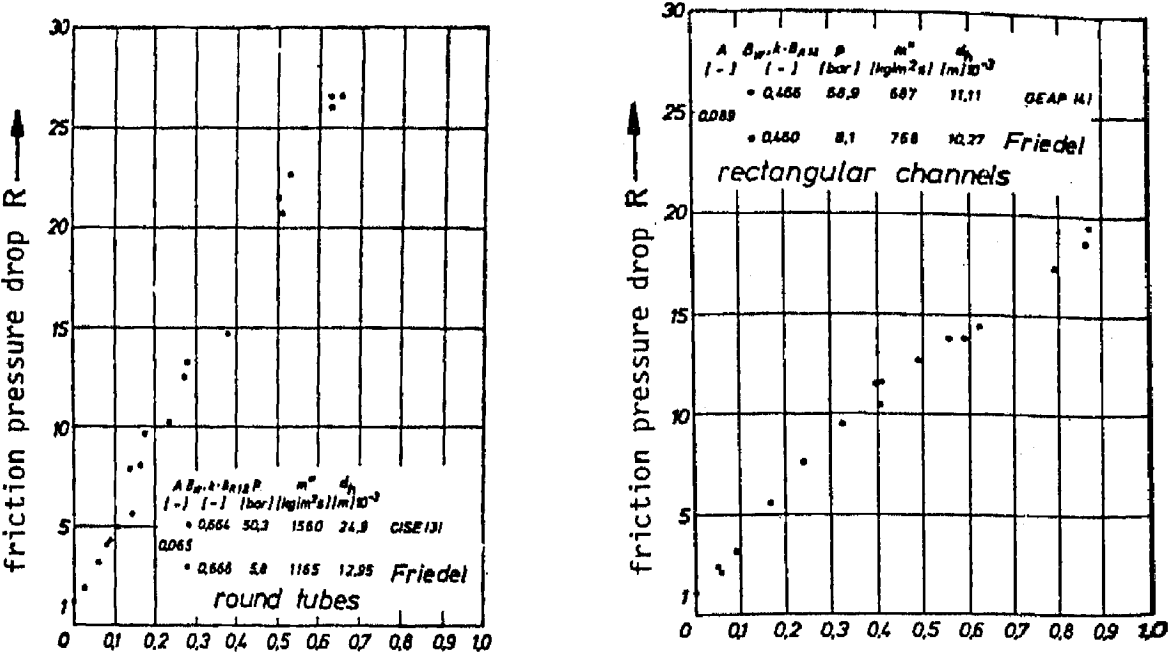


Fig. 10. Two-phase flow pressure drop multiplier scaled according to Friedel [12].

position is a little better with the thin liquid film at the wall through which the heat is transported by conduction and convection. Based on a proposal of Shrock and Grossmann [13] the ratio of the heat transfer coefficients in two-phase flow and in single phase flow is given as a function of the Martinelli-parameter and of the boiling number.

$$\frac{\alpha_{2ph}}{\alpha_{1ph(liquid)}} = C_1 \left[N_{Bo} \cdot 10^4 + C_2 \left(\frac{1}{X} \right)^m \right]^m \tag{19}$$

The heat transfer of the single phase-liquid flow can be calculated from the well known correlations in the literature usually containing the Reynold-number and the Prandtl-number. So scaling for this phenomenon should work if we select the Martinelli-parameter, the boiling-number and the quality correctly. But comparing heat transfer coefficients measured in Freon, organic fluid and water the empirical constants in equation 19

always have to be adjusted separately as Calus [14] showed. Future experiments have to clarify whether there is an additional scaling parameter to be taken into account.

Heat transfer with spray- or fog-cooling, i.e. in the fourth above-mentioned region sometimes plays an important role in engineering practice as for example in the superheating part of a boiler or during the emergency core cooling of a nuclear reactor. Scaling these heat transfer conditions is a not too serious problem, because the heat transfer coefficient is mainly governed by the vapour flow and the liquid droplets are only cooling the boundary layer near the wall and so improving the heat transport. Dimensionless groups for modelling therefore are a modified Reynolds-number and the Prandtl-number related to the vapour phase. A well known correlation is the equation of Dougall-Rohsenow.

$$\begin{aligned} \text{Nu} &= 0,023 \text{Re}^{0,8} \text{Pr}_g^{0,4} \\ \text{Re} &= \frac{\dot{m} d_h}{\eta_g} \left[\dot{x} + \frac{\rho_g}{\rho_l} (1 - \dot{x}) \right] \end{aligned} \quad (20)$$

Scaling criteria are the Reynolds-number as defined in equation 20, the Prandtl-number of the vapour, and the quality of the fluid. Comparisons with experimental data measured in water and Freon gave quite good results and good agreement with Dougall-Rohsenow's correlation. From this example we learn that always this phase, which governs the fluiddynamic or heat transfer process has to be adjusted in its thermodynamic properties.

5. SCALING COMBINED PHENOMENA

The fluiddynamic behaviour in an engineering apparatus like a boiler, a nuclear reactor or distillation and extraction columns is a very strongly combined effect of several simple phenomena and usually fluid flow and heat transfer are linked together. The heat transferred to the fluid determines the void fraction, the produced vapour influences the pressure drop, which governs the mass flow rate and this again can effect the heat transfer. Up to now we regarded only each single simple phenomenon separately assuming no influence from other processes.

Out of the numerous problems of technical two-phase flow for discussion here we select the burnout behaviour and the blowdown conditions during a loss of coolant accident in a nuclear reactor. Other problems will be presented by Ishii in

the following paper.

The exact knowledge of the critical heat flux with boiling (burnout or dryout) is an urgent problem in the layout of the fuel elements of water cooled nuclear reactors. Due to the high heat input and the extensive instrumentation the experiments are very expensive. Therefore it was obvious to look for more convenient and cheaper test conditions. Here Freon as a modelling fluid seemed to offer a possibility. There are several proposals in the literature for scaling critical heat flux from Freon to water. All start from the thermodynamic condition that the density ratio of liquid and vapour has to be the same in the modelling and in the original fluid.

Stevens [15,16] preferred a more empirical procedure and made a direct comparison of the burnout data in Freon and water with simple scaling factors. He postulated that in addition to the same density ratio and the identical geometry the quality (or subcooling) at the inlet and the outlet of the heated length have to be the same in the model and in the original. Therefore only the mass flow rate remains as free variable to be adjusted in the scaled down conditions. This scaled mass flow rate is got via the scaling factor K by plotting the quality $\dot{x}_A$ (at the outlet) versus the parameter

$$\left[\dot{m} \cdot d_h^{0.25} \cdot \left(\frac{d_h}{l} \right)^{0.59} \right]$$

as this is done in fig. 11 with the help of measurements in a rod cluster which were carried out by Hein and Kastner [17].

Barnett [18] used the dimensionless analysis for deriving his scaling laws. He listed all parameters, which are according to the status of knowledge mainly governing the physical behaviour of the phenomenon and others which have a minor influence. Doing so, he gets a relation of the form

$$q_{CHF} = f(d, l, \dot{m}, p, \Delta h, h_{lg}, \rho_l, \rho_g, c_l, \lambda_l, v_l, \sigma, \frac{d(\rho_l/\rho_g)}{dp}) \quad (21)$$

generally describing the critical heat flux. Adapting the dimensional analysis equation 21 can be rearranged in the form of dimensionless groups and he gets

$$\frac{q''}{h_{lg}^{1.5} \rho_g} = f \left(\frac{l}{d}, \frac{D \cdot \rho_g \cdot h_{lg}^{0.5} c_{pF}}{\lambda_l}, \frac{\dot{m}}{\rho_g h_{lg}^{0.5}}, \frac{\Delta h}{h_{lg}}, \frac{\rho_l}{\rho_g}, \frac{v_l \cdot \rho_g \cdot c_{p_l}}{\lambda_l}, \frac{\sigma \cdot c_{p_l}}{h_{lg}^{0.5} \cdot \lambda_l}, h_{lg} \cdot \rho_g \cdot \frac{d(\rho_l/\rho_g)}{dp_s} \right) \quad (22)$$

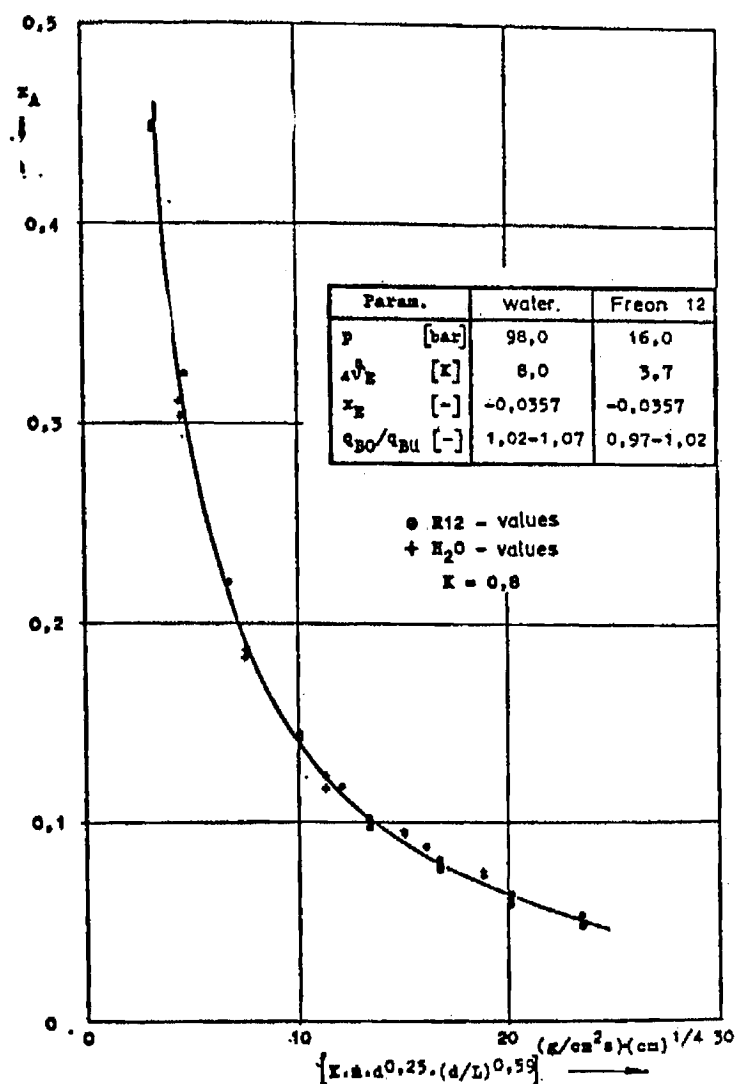


Fig. 11. Stevens' [15] burnout scaling factor for mass flow

From these groups in equation 22 Barnett developed several scaling factors N_n depending which thermodynamic properties he was taking in account in addition to the values of latent heat of evaporation h_{lg} and density of liquid and vapour ρ_l, ρ_g .

Examples of sets for scaling factors elaborated by Barnett with this method are shown in fig. 12. Barnett offers several possibilities for scaling critical heat flux depending which combination of thermodynamic properties is assumed to be the most appropriate one.

Bouré was the first, who clearly stated that a comprehensive scaling of the critical heat flux is not possible and that only a restricted similarity of the boiling crisis phenomenon in water and in Freon may exist. Realizing this he emphasised his study to elaborate strict rules for a limited similarity.

$$q'' = f \left(l, d, \dot{m}, p, \Delta h, h_{lg}, \rho_l, \rho_g, c_{pl}, \lambda_l, \nu_l, \sigma, \frac{d(\rho_l/\rho_g)}{dp_s} \right)$$
$$\gamma = \frac{d(\rho_l/\rho_g)}{dp_s} \qquad \beta = \frac{d\gamma_s}{dp_s}$$

No.	properties	equation $q'' = f(l, d, \dot{m}, p, \Delta h)$	F_q	$F_{d,l}$	$F_{\dot{m}}$	$F_{\Delta h}$
4	$h_{lg}, \rho_l, \rho_g, c_{pl}, \lambda_l, \gamma$	$\frac{q'' \cdot \gamma^{0.5}}{\lambda_l \cdot \sqrt{\rho_l}} = f \left(\frac{1}{d}, \frac{d \cdot c_{pl} \cdot \sqrt{\rho_l}}{\lambda_l \cdot \gamma^{0.5}}, \frac{\dot{m} \cdot \gamma^{0.5}}{\sqrt{\rho_l}}, \frac{\rho_l}{\rho_g}, \frac{\Delta h}{h_{lg}} \right)$	22,43	0,717	1,914	11,72
5	$h_{lg}, \rho_l, \rho_g, \beta, \lambda_l, \gamma$	$\frac{q'' \cdot \gamma^{0.5}}{h_{lg} \cdot \sqrt{\rho_l}} = f \left(\frac{1}{d}, \frac{d \cdot h_{lg} \cdot \gamma^{0.5} \sqrt{\rho_l}}{\beta \cdot \lambda_l}, \frac{\dot{m} \cdot \gamma^{0.5}}{\sqrt{\rho_l}}, \frac{\rho_l}{\rho_g}, \frac{\Delta h}{h_{lg}} \right)$	22,43	0,482	1,914	11,72
10	$h_{lg}, \rho_l, \rho_g, \mu_g, \gamma$	$\frac{q'' \cdot \gamma^{0.5}}{h_{lg} \cdot \sqrt{\rho_l}} = f \left(\frac{1}{d}, \frac{d \cdot \sqrt{\rho_l}}{\mu_g \cdot \gamma^{0.5}}, \frac{\dot{m} \cdot \gamma^{0.5}}{\sqrt{\rho_l}}, \frac{\rho_l}{\rho_g}, \frac{\Delta h}{h_{lg}} \right)$	22,43	0,814	1,914	11,72
12	$h_{lg}, \rho_l, \rho_g, c_{pg}, \lambda_g, \beta$	$\frac{q'' \cdot \sqrt{\beta \cdot c_{pg}}}{h_{lg}^{1.5} \cdot \rho_l} = f \left(\frac{1}{d}, \frac{d \cdot \sqrt{c_{pg} \cdot h_{lg} \cdot \rho_l}}{\lambda_g \cdot \sqrt{\beta}}, \frac{\dot{m} \cdot \sqrt{\beta \cdot c_{pg}}}{\sqrt{h_{lg} \cdot \rho_l}}, \frac{\rho_l}{\rho_g}, \frac{\Delta h}{h_{lg}} \right)$	23,06	0,317	1,968	11,72

Fig. 12. Scaling factors for critical heat flux according to Barnett [18].

He distinguishes - similar as Barnett - two groups of parameters: primary parameters and secondary ones. He used the later ones to determine correction factors for the primary parameters. Doing so he obtained the following 4 dimensionless groups.

$$N_1 = K_1 \frac{\rho_l}{\rho_g} \quad ; \quad N_2 = K_2 \frac{\Delta h_{int}}{h_{lg}}$$
$$N_3 = K_3 \frac{\dot{q} \cdot l}{h_{lg} \cdot \dot{m} \cdot d} \quad N_4 = K_4 \frac{\dot{m}}{\rho_l \sqrt{g l}}$$

(23)

The correction- or scaling factors $K_1 - K_4$ are depending from the geometry of the channel as well as from the pressure. The values of two of them can be chosen arbitrarily and by using the same density ratios of liquid and vapour in water and in Freon the factor K_1 becomes unit. The scaling factor K_4 may vary in the order from 1 to 2.5 and by fixing this factor the scaling factors K_2 and K_3 can be taken from fig. 13.

Finally we have to mention the method proposed by Ahmad [20] who also subdivided the parameters in groups, namely system describing, primary and secondary parameters. He gets 13 dimen-

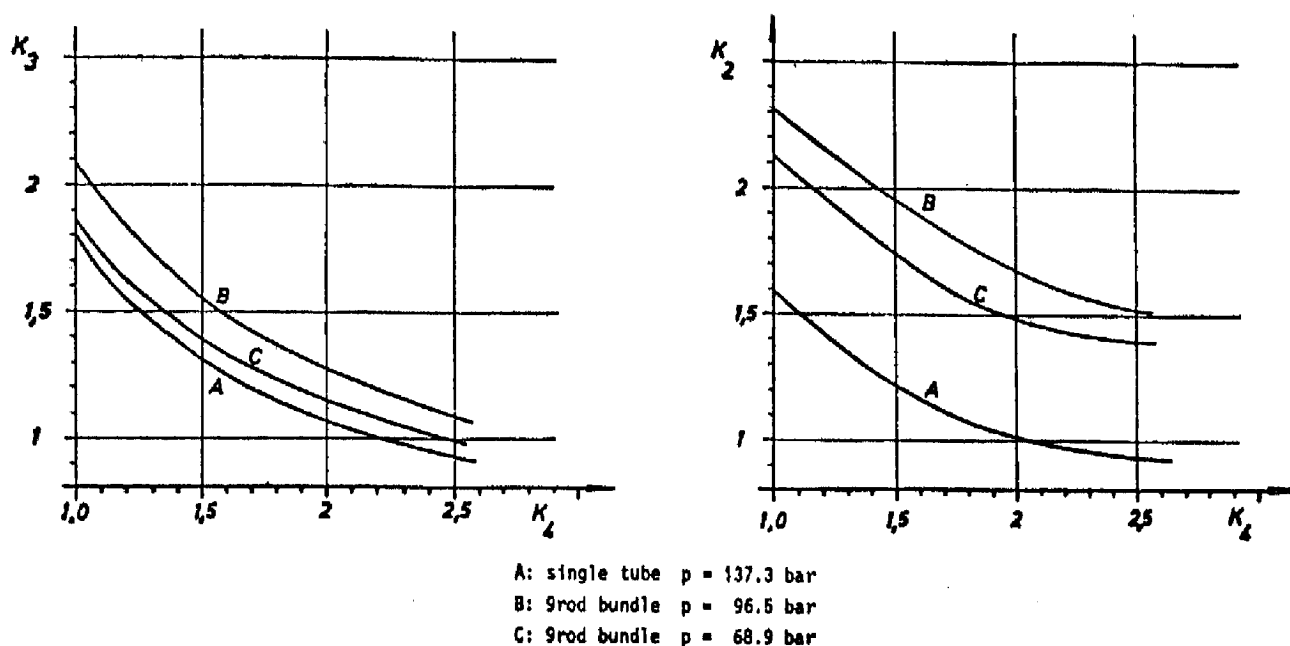


Fig. 13. Scaling factors for critical heat flux, according to Bouré.

sionless numbers from which he selects 3 for restricted scaling arranging them as a function of the modelling parameter

$$\psi = f \left(\frac{\dot{m} \cdot d}{\eta_l}, \frac{\eta_l}{\sigma \cdot d \cdot \rho_l}, \frac{\rho_l}{\rho_g} \right) \quad (24)$$

In addition he gives a function for the modified boiling number (see fig. 2)

$$N_{Bo}^* = \frac{\dot{q}}{\dot{m} \cdot h_{lg}} = f \left(\psi, \frac{\Delta h_{sub}}{h_{lg}}, \frac{\rho_l}{\rho_g}, \frac{1}{d} \right) \quad (25)$$

and from experiments he empirically finds the following relationship between the scaling numbers:

$$\psi = \left(\frac{\dot{m} \cdot d}{\eta_l} \right) \left(\frac{\eta_l}{\sigma \cdot d \cdot \rho_l} \right)^{n_1} \left(\frac{\rho_l}{\rho_g} \right)^{n_2} \quad (26)$$

Rearranging the terms in equation 26 we realize that the modelling parameter ψ is a function of well-known dimensionless numbers

$$\psi = \underbrace{\left(\frac{\dot{m}^2 \cdot d}{\rho_l \cdot \sigma} \right)^{0.67}}_{We} \cdot \underbrace{\left(\frac{\dot{m} \cdot d}{\eta_l} \right)^{-0.133}}_{Re_l^*} \cdot \underbrace{\left(\frac{\dot{m} \cdot d}{\eta_g} \right)^{-0.2}}_{Re_g^*} \quad (27)$$

So in addition to Barnett's and Bouré's energy orientated dimensionless groups Ahmad introduced hydrodynamic scaling numbers.

Before we check the validity of these scaling laws for critical heat flux we have to remind that the uncertainty of burn-out measurements is in the order of $\pm 10\%$. The best agreement between scaled and original data can be found for simple geometries of course. With inside cooled uniformly heated tubes agreement within $\pm 7\%$ was realized. More interesting for practical use but also more complicated due to additional influencing hydrodynamic parameters is the scaling of critical heat flux for rod bundles, Hein and Kastner [17] compared own measurements in water and Freon and scaled them according to Bouré

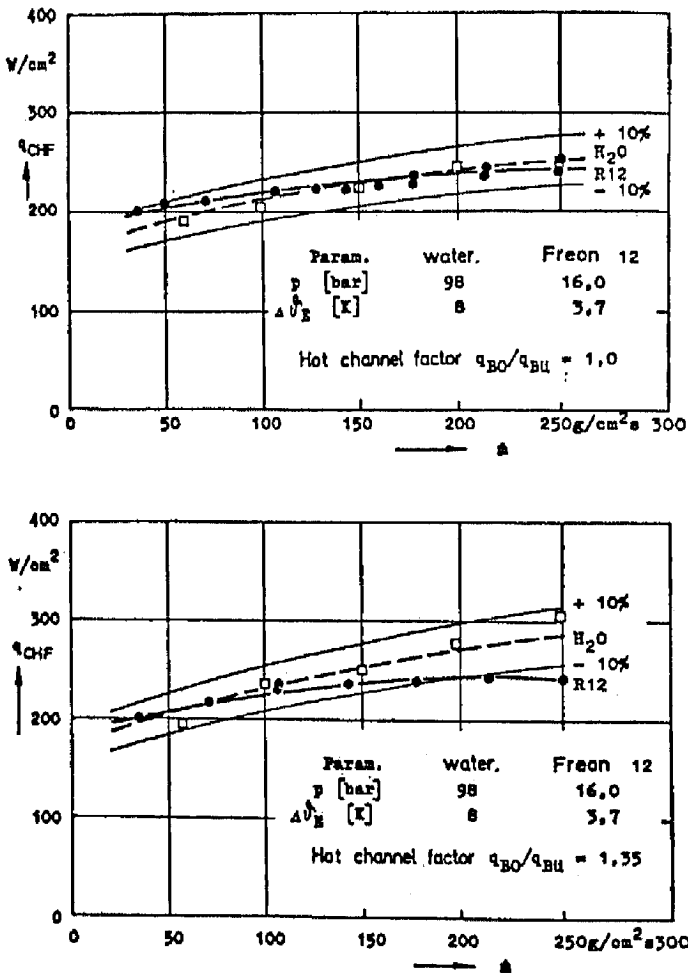


Fig. 14. Influence of mass flow rate and radial power distribution on critical heat flux scaling (Bouré).

as shown in fig. 14. They found that there is an influence of the mass flow rate on the factor K_3 (see equation 23), which scales the critical heat flux from Freon to water. The tests in fig. 14 were done with a 9-rod cluster. The influence of the mass flow rate is relatively small if all 9 rods have the same heat flux, i.e. if there is uniform heat flux distribution. With increasing hot channel factor the deviation of the scaled values become greater, which is probably due to a mixing effect between the subchannels not being taken into account in the scaling deliberations. This is a clear hint for the restrictive similarity.

For uniform heat flux distribution water and Freon data can be easily brought in agreement by a simple mass flow dependent correcting function proposed by Hein and Kastner [17] as demonstrated in fig. 15. It has to be mentioned that in this comparison a correction taking into account the pressure dependency of the scaling factor, which was proposed later by Courtaud and De Bousquet is not yet considered. For more detailed information on the agreement between scaled and measured data of critical heat flux it may be referred to a paper by Hein [21, 17].

From the comparison in fig. 14 we learned that hydrodynamic

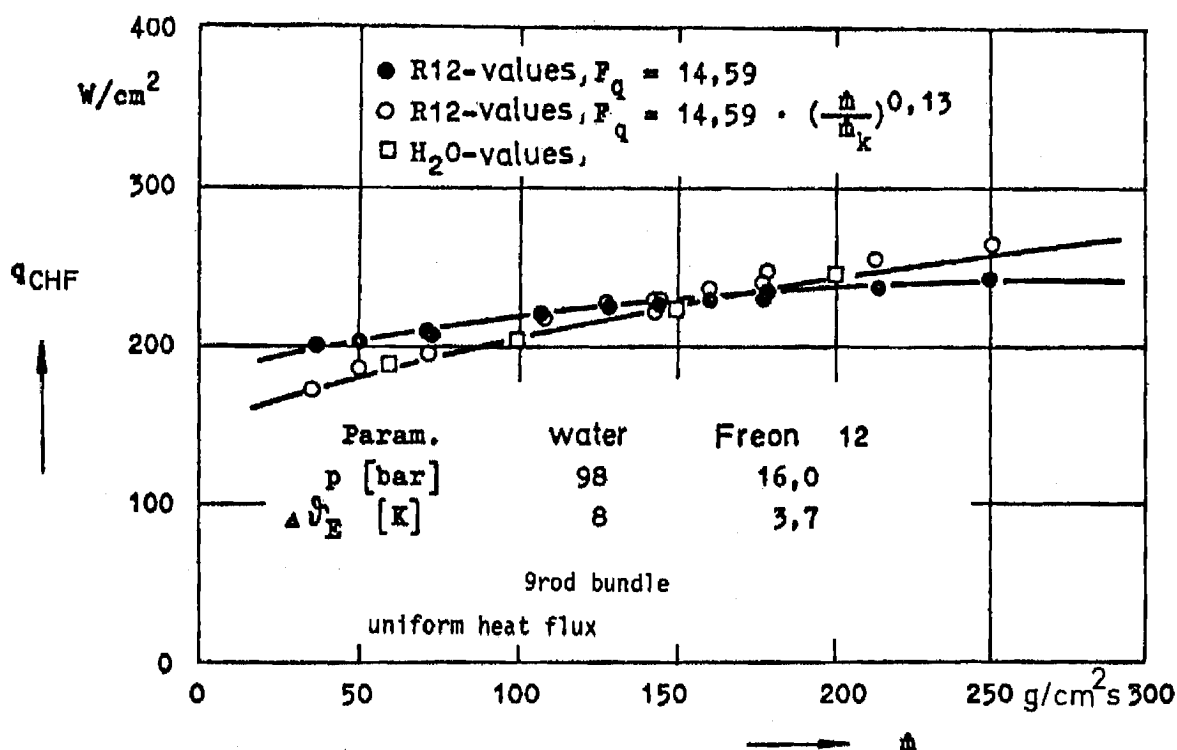


Fig. 15. Mass flow correction for critical heat flux scaling (Bouré, Hein).

phenomena like mixing may have a strong influence on critical heat flux scaling. The first reaction on this problem may be to simulate all hydrodynamic conditions as good as possible, i.e. to use exactly the same hot channel factor in the water and in the Freon test. This however, presupposes, that the similarity conditions for mixing and for critical heat flux are the same else we can only scale one of both correctly. From this we can draw the conclusion, that - generally spoken - scaling with dimensionless numbers only is not sufficient in two-phase flow. We need a theoretical description of the whole thermodynamic and fluiddynamic process, predicting the behaviour in the model as well as in the original set-up.

The circumstances become even more complicated if we consider transient conditions for example the thermohydraulic behaviour of the two-phase flow during a blowdown due to a loss of coolant accident in a reactor. Doing experimental research work for investigating the fluid dynamic and heat transfer aspects of this problem we are forced to scale even using water in our experimental set-up, because the rod bundle in the test can only be a very small section of a whole reactor core, i.e. we have a geometrical scale down. The number of rods tested is usually limited by the total power input available to heat them. If we use Freon instead of water we can multiply the number of rods by a factor of approximately 15. But then we have to ask how to scale from Freon to water in addition.

Blowdown tests with Freon were made in our laboratory and compared with blowdown measurements performed with water by a German manufacturer of nuclear reactors [23]. The conditions in the Freon loop were very carefully adapted and scaled to the water test rig. There was a two fold purpose of these measurements namely to study the burnout delay time during blowdown and to determine the heat transfer coefficient in postdryout conditions. Depending which of these two phenomena are intended to scale one gets different similarity terms. Here we just want to discuss a little more detailed the dryout delay scaling.

The blowdown occurrence is too complex to overcome the scaling problems simply by using dimensionless numbers. One has to develop a physical conception of the thermohydraulic events and formulate it in mathematical expressions as differential equations. Due to the rapidly reduced pressure flashing and then a very high acceleration directed to the break occurs in the fuel elements. In case of a large break in the primary system of a pressurized water reactor the pressure would be reduced within about 20 s from 150 to approximately 5 bar. Emphasis has to be given to imitate in the Freon loop these very severe flashing conditions and the resulting acceleration of the fluid. The acceleration can be guaranteed by adapting the same local and

temporal pressure ratio, which can be done by lowering the outside pressure of the Freon loop to about 0.1 bar. Then we still have the problem of critical (sonic) mass flow rate and different heat storage conditions in the Freon and in the water loop. All these problems can only be overcome by a detailed theoretical analysis used as basis for scaling. This analysis has to predict the results of Freon tests and the water tests as well. The scaling is not done from one experimental condition to the other but both test results are compared with theoretical predictions.

The tests were done for boiling water reactor conditions, where vapour is present already in steady state operation. The liquid phase is flowing along the heated wall and the vapour is concentrated in the bulk between the rods. The dryout, i.e. the disappearance of the liquid layer at the wall then is caused by the following effects:

1. Evaporization (heat flux from the rods)
2. Flashing due to pressure decrease
3. Entrainment due to high vapour velocity

We can describe the whole procedure with the well known constitution equations for mass, energy and momentum. In addition one needs information on the slip ratio because the difference in the phase velocity produces entrainment.

Belda [3] developed an analysis on this basis starting from the equations given in fig. 16 and using for the phase velocities the equations derived from pressure drop deliberations as pointed out in fig. 17. The entrainment behaviour during the transient process was tried to be predicted by aid of investigations carried out by Hewitt [26]. With this mathematical treatment he gets a differential-integral equation describing the film thickness as a function of time and place.

$$\frac{d}{dz} \left[(\rho_l w_l (1-c)(1-e) + \rho_l w_E (1-c)e) + \frac{d}{dz} (\rho_g w_g c) + \frac{d}{dt} [(\rho_l (1-c)(1-e) + \rho_l (1-c)e + \rho_g c)] \right] = 0$$

$$\frac{h_l}{h_g} \frac{d}{dz} \left[(\rho_l w_l (1-c)(1-e) + \rho_l w_E (1-c)e) + \frac{d}{dz} (\rho_g w_g c) + \frac{1}{h_g} \frac{d}{dt} [(\rho_l (1-c)(1-e) + \rho_l (1-c)e) h_l + (\rho_g c h_g)] \right] = \dot{q}(z) \frac{U}{A_T} \frac{1}{h_g}$$

$$\dot{M}_l = \rho_l A_T (1-c)(1-e) \cdot w_l$$

$$\dot{M}_E = \rho_l A_T (1-c)e \cdot w_E$$

Fig. 16. Mass and energy equation for dryout delay during blow-down.

Velocities of phases

$$w_{ph} = \sqrt{\left(\frac{dp}{dz}\right)_{ph} \cdot \frac{2 d_h}{\xi \cdot \rho_{ph}}}$$

$$\left(\frac{dp}{dz}\right)_{ph} = \frac{1}{\rho_{ph}^2} \cdot \left(\frac{dp}{dz}\right)_{2-ph}$$

$$\frac{1}{\rho_l^2} = (1 - \epsilon)^2 \quad \frac{1}{\rho_g^2} = \frac{\epsilon^{2.5}}{1 + 75 \cdot (1 - \epsilon)}$$

$$w_l = \sqrt{\frac{A_l}{A_T} \cdot \left(\frac{dp}{dz}\right)_{2-ph} \cdot \frac{2 d_h}{\xi_l \cdot \rho_l}}$$

$$w_g = \sqrt{\frac{A_T \cdot (A_T - A_l)}{A_T - 75 A_l} \cdot \left(\frac{dp}{dz}\right)_{2-ph} \cdot \frac{2 d_h}{\xi \cdot \rho_g}}$$

Fig. 17. Dryout delay during blowdown, equations describing phase velocities.

$$\frac{1}{\rho_l \cdot l} \left(\dot{M}_l(l, t) - \dot{M}_l(0, t) + \dot{M}_E(l, t) \right) + \frac{\partial A_l}{\partial t} + A_l \cdot \left(\frac{1}{\rho_g} \cdot \frac{\partial \rho_l}{\partial t} + \right.$$

$$\left. \frac{1}{h_{lg}} \left(\frac{\rho_g}{\rho_l} \cdot \frac{\partial h_g}{\partial t} + \frac{\partial h_l}{\partial t} \right) \right) + A_{ges} \left(\frac{I \dot{q}(z) \cdot dz \cdot U_b}{\rho_l \cdot h_{lg} \cdot l \cdot A_{ges}} - \frac{\rho_g}{\rho_l} \cdot \frac{1}{h_{lg}} \cdot \frac{\partial h_g}{\partial t} \right) = 0 \quad (28)$$

In equation 28 the local and temporal values of mass flow rate and quality in the fuel element or in the test section have to be known from blowdown calculations, which can be performed for example with the well known computer codes like RELAP IV or BRUCH. We then can determine from equation 28 at what time after the break the liquid layer at a certain position of a rod in the bundle would become zero, which means that the dryout occurs. For adapting the Freon tests conditions one can derive from equation 28 and from the equations in fig. 16 and 17 dimensionless scaling numbers, too. They are listed in fig. 18. From this figure we can see that the system pressure is four times over determined. We therefore have to decide, which of these four expressions is the dominant one. It can be easily seen that the dependance of the liquid enthalpy from pressure is much smaller than the change of latent heat of evaporization with pressure. So two of the conditions can be ruled out and the remaining two fortunately give quite similar values in the order of 0.19. But there is a 5th condition because we decided to scale with the critical pressure ratio and from this we get the

heat flux	$K_1 = \frac{\dot{q}(z) \cdot l \cdot U_B}{\dot{m}_{GES} \cdot A_{GES} \cdot h_{lg}}$
pressure	$K_{21} = \frac{p_s}{\rho_l} \cdot \frac{\partial \rho_l}{\partial p}$ $K_{23} = \frac{p_s}{h_{lg}} \cdot \frac{\rho_g}{\rho_l} \cdot \frac{\partial h_l}{\partial p}$ $K_{22} = \frac{p_s}{h_{lg}} \cdot \frac{\partial h_l}{\partial p}$ $K_{24} = \frac{p_s}{h_{lg}} \cdot \frac{\partial h_{lg}}{\partial p}$
acceleration	$K_3 = \frac{\Delta p \cdot \rho_l}{\dot{m}_{GES}^2} = Eu_l$ $K_4 = \frac{\Delta p \cdot \rho_g}{\dot{m}_{GES}^2} \cdot \frac{\rho_g}{\rho_l} = Eu_g \cdot \frac{\rho_g}{\rho_l}$
mass flow rate	$K_5 = \zeta_l \approx Re = \frac{\dot{m}_{GES} \cdot d}{\eta_l}$
geometry	$K_6 = \frac{\sqrt{A_{GES}}}{l} \approx \frac{d_h}{l}$

Fig. 18. Dimensionless groups for dryout delay scaling during blowdown (Belda).

value 0.188. So finally 0.19 could be chosen as a good compromise.

By scaling the hydrodynamic and thermodynamic conditions in the Freon loop before and during the blowdown with the dimensionless numbers given in fig. 18 we got a quite good agreement between water and Freon behaviour as can be seen from fig. 19, where the temporal course of system pressure, mass flow rate and void fraction and the pressure drop in the fuel element are plotted for water and for Freon versus the blowdown time. This conformity, however, does not mean that the dryout delay time are the same in Freon and in water because we have only made the hydrodynamic side of the process analogous and we could not completely scale thermodynamic details for example stored heat in the construction materials and the complete interference between thermodynamic and hydrodynamic properties. This means we have to do an indirect scaling by comparing the measured data with the theoretically predicted ones. As fig. 20 demonstrates there is good agreement between measured and predicted dryout delay time. The comparison was done for different locations of the break - in the hot and in the cold leg of the primary system - for a variety of break areas and for different heat flux densities in the moment before the accident occurs.

Starting from fundamental deliberations the theoretical approach should predict the behaviour in water as well as in Freon. Unfortunately there are available only very few water tests

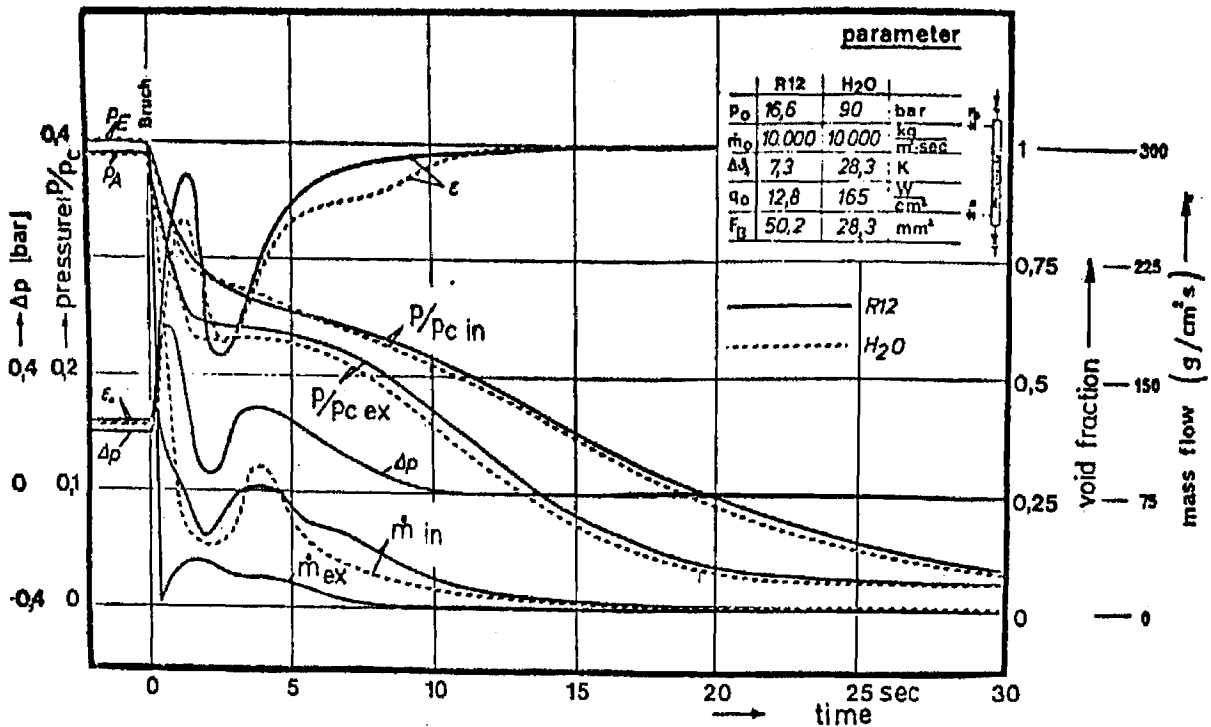


Fig. 19. Blowdown during loss of coolant accident, comparison between water tests and scaled Freon 12 data.

where the dryout delay time during blowdown was measured and where in addition the temporal course of the hydrodynamic conditions in the fuel elements is reliably known. Comparison with water experimental data at hand show good agreement with the theory as can be seen from fig. 21. This encourages to draw the conclusion that scaling on the detour of a theoretical analysis is a promising procedure for combined and complicated two-phase flow phenomena.

To support this a comparison between measured Nusselt-numbers in water and Freon during blowdown may be shown in fig. 22 without discussing the scaling laws for this special problem. In this figure measurements done with water [23] and with Freon [24] are compared with correlations. Keeping in mind, that there are many uncertainties arising from the measuring technique the agreement is satisfactorily. It has to be added, that the comparison can be made only in the period between 5 and 12 s after the break appears, because before we have transition boiling for which the used scaling model is not valid and afterwards the hydrodynamic conditions in the water and in the Freon loop differ considerably.

There is certainly a lot of other complicated two-phase flow problems which are of great technical interest. I should mention

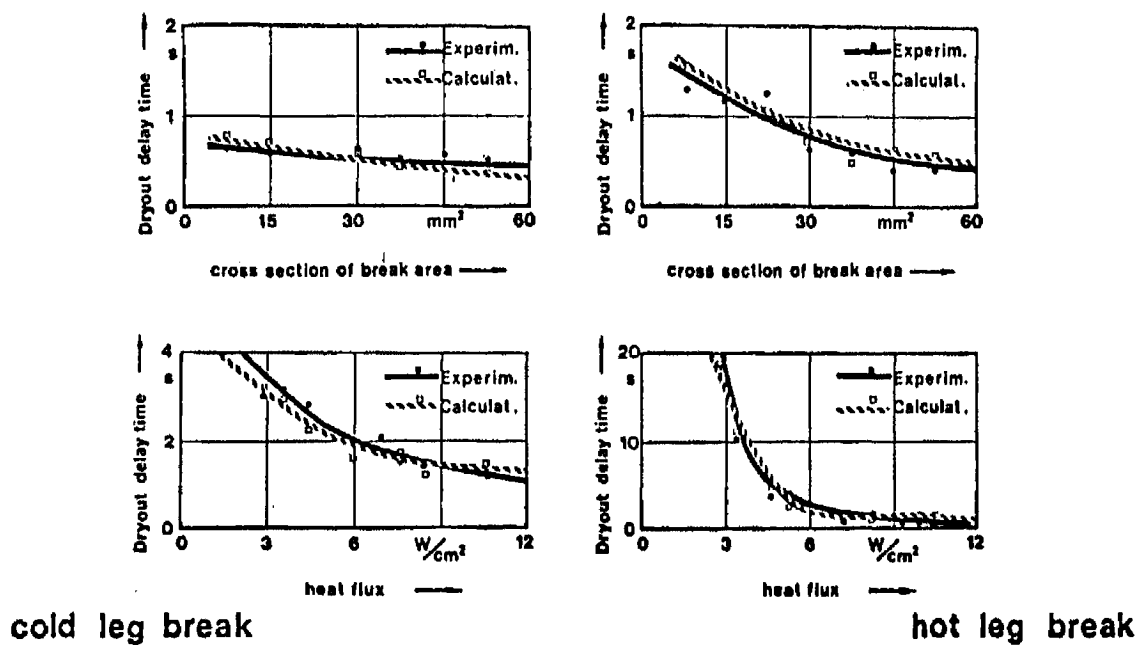


Fig. 20. Dryout delay time, measured (in Freon 12) and calculated data.

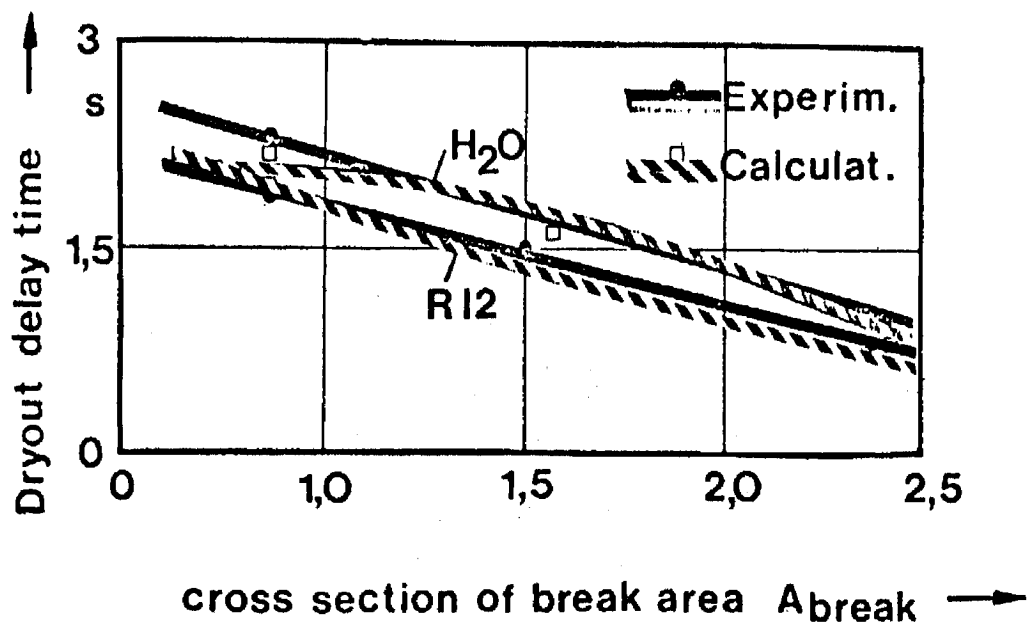


Fig. 21. Dryout delay time, comparison of experimental and theoretical data for water and for Freon 12.

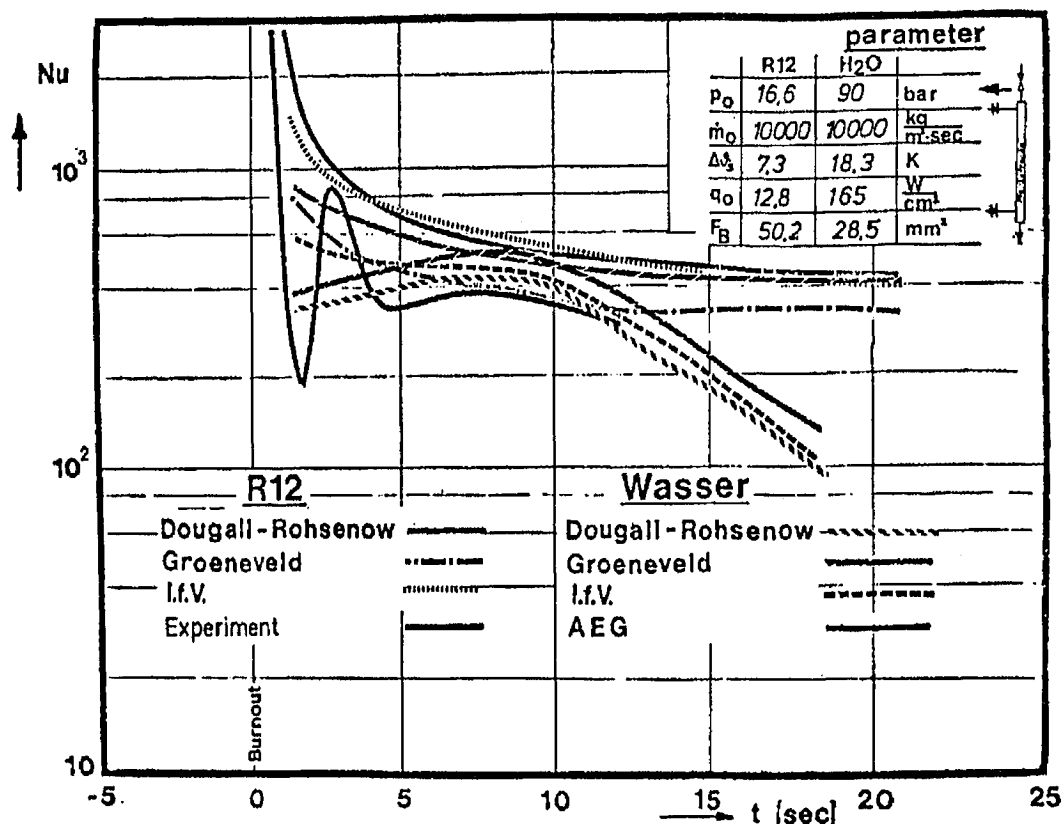


Fig. 22. Heat transfer in post dryout conditions during blow-down, comparison of water data and scaled Freon data.

the phenomena of subcooled boiling, of flow oscillations and instabilities and the interchannel mixing.

5. CONCLUSION

Even in single phase flow scaling is restricted under certain circumstances as we have seen in the example of combined forced and free convection. This limitation becomes much stronger in two-phase flow. Whilst in a single phase fluid we have usually similarity for hydrodynamic and heat transfer processes simultaneously, in two-phase flow each modelling law or scaling number is only valid for a single special phenomenon.

Scaling only with the help of dimensionless numbers is limited in two-phase flow to simple and isolated problems, where the physical phenomenon is a unique function of a few parameters. If there is a reaction between two or more physical occurrences, dimensionless scaling numbers mainly serve for selecting the hydrodynamic and thermodynamic conditions of the modelling tests and we have to separate the influencing parameters in primary

ones determining the system and secondary ones which are of minor influence.

In not too complicated cases scaling to the original circumstances can be done by empirical correlations considering the important physical laws of the process. For many technical applications in future we shall be forced to scale via a computer code which analyses and describes the thermohydraulic phenomena as good as possible.

This makes it necessary to get a better understanding of the thermohydraulic behaviour in two-phase flow systems. A better theoretical approach would also help us to generalize experimental data and such to make full use of the numerous experimental results in two-phase flow, which up to now stand to a great extend apart and uncomparable. So scaling is not only an expedient to save expenses for experimental research work, it also helps to compare and generalize measured data. Elaborating scaling laws for two-phase flow we have to put more effort to the theoretical analysis of this process.

NOMENCLATURE

c	specific heat
d	diameter
g	acceleration of gravity
h	enthalpy
h_{lg}	latent heat of evaporation
l	length
m	mass flow rate
M	mass flow
p	pressure
Δp	pressure drop
q, q''	heat flux
s	slip
T	temperature
v	volume
w	velocity
$\bar{x}$	quality
x, y, z	length coordinates

GREEK SYMBOLS

α	heat transfer coefficient
ϵ	void fraction
η	viscosity
ψ	two-phase parameter

ρ	density
σ	surface tension
ν	kinematic viscosity

DIMENSIONLESS GROUPS

Fr	Froude-Number
Gr	Grashof-Number
N	bubble-number
N _{BO}	boiling-number
Nu	Nusselt-Number
Pr	Prandtl-Number
Re	Reynolds-Number

SUBSCRIPTS

c	critical
CHF	critical heat flux
g	gas
h	hydrodynamic
H ₂ O	water
m	inlet
l	liquid
lg	evaporation
m	model
o	original
s	saturation
sub	subcooling

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